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Amir Karton and Jan M. L. Martin

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The lowest singlet-triplet excitation energy of BN: A converged coupled cluster perspective

Amir Karton and Jan M. L. Martin^{a)}

Department of Organic Chemistry, Weizmann Institute of Science, IL-76100 Rehovot, Israel

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The notoriously small $X^3\Pi - a^1\Sigma^+$ excitation energy of the BN diatomic has been calculated using high-order coupled cluster methods. Convergence has been established in both the one-particle basis set and the coupled cluster expansion. Explicit inclusion of connected quadruple excitations $\hat{T}_4$ is required for even semiquantitative agreement with the limit value, while connected quintuple excitations $\hat{T}_5$ still have an effect of about 60 cm^{-1} . Still higher excitations only account for about 10 cm^{-1} . Inclusion of inner-shell correlation further reduces T_e by about 60 cm^{-1} at the CCSDT, and 85 cm^{-1} at the CCSDTQ level. Our best estimate, $T_e = 183 \pm 40\text{ cm}^{-1}$, is in excellent agreement with earlier calculations and experiment, albeit with a smaller (and conservative) uncertainty. The dissociation energy of $\text{BN}(X^3\Pi)$ is $D_e = 105.74 \pm 0.16\text{ kcal/mol}$ and $D_0 = 103.57 \pm 0.16\text{ kcal/mol}$.

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I. INTRODUCTION

The lowest electronic excitation energy of the boron nitride diatomic is among the most vexing problems in small-molecule computational chemistry. Not only are the $X^3\Pi$ and $a^1\Sigma^+$ states nearly degenerate but the combination of moderate multireference character in the $X^3\Pi$ state and pathological multireference character in the $a^1\Sigma^+$ state makes the transition energy T_e excessively sensitive to the electron correlation treatment.

Martin *et al.*,¹ using multireference average coupled pair functional (ACPF) techniques,³ found the $^3\Pi$ state to be the ground state and predicted $T_e = 381 \pm 100\text{ cm}^{-1}$. These authors also found that (nowadays) commonly used coupled cluster methods such as CCSD(T) (Ref. 4) yield qualitatively incorrect answers. Elaborate multireference calculations by Mawhinney, Bruna, and Grein (MBG),² by Peterson,⁵ and by Bauschlicher and Partridge⁶ (BP) obtained considerably lower T_e values of 241 ± 160 , 190 ± 100 , and $180 \pm 110\text{ cm}^{-1}$, respectively. Watts,⁷ at the coupled cluster with all single, double, and triple excitations,⁸ (CCSDT) level with a correlation consistent polarized quadruple zeta¹⁷ (cc-pVQZ) basis set, found $T_e = 844\text{ cm}^{-1}$ and conjectured that this serious overestimate was due to neglect of connected quadruple ($\hat{T}_4$) and higher excitations. Both Boese *et al.*⁹ and Tajti *et al.*,¹⁰ in the context of high-accuracy computational chemistry protocols developed in their papers, found that, in strongly multireference systems, $\hat{T}_4$ can easily make energetic contributions on the order of the difference between the CCSDT and multireference values. (Denis¹¹ crudely estimated the effect of $\hat{T}_4$ by assuming error cancellation with higher-order $\hat{T}_3$ in the singlet but not the triplet state and predicted $T_e = 175\text{ cm}^{-1}$.) Finally, a very recent quantum Monte Carlo

(QMC) study by Lu¹² in the present journal found $178(83)\text{ cm}^{-1}$, where the uncertainty band represents one standard deviation in the QMC approach.

The two most reliable experimental estimates are the noble gas matrix IR measurements of Lorenz *et al.*,¹³ $15\text{--}182\text{ cm}^{-1}$, and the negative ion time-of-flight photoelectron spectroscopy value of Asmis *et al.*,¹⁴ $158 \pm 36\text{ cm}^{-1}$.

The purpose of the present work is to establish whether a converged result can be obtained at all from single-reference coupled cluster methods, whether this estimate is in agreement with the other theoretical approaches and experiment, and finally what is the breakdown of various contributions in the cluster expansion.

II. COMPUTATIONAL DETAILS

All calculations were carried out using the general coupled cluster code MRCC of Kállay.¹⁵ The Austin-Mainz version of ACES II (Ref. 16) was used to generate the required integrals and molecular orbitals. Unless otherwise noted, the CCSDT/cc-pVQZ reference geometries of Watts⁷ were used, $r_e(X^3\Pi) = 1.3302$ and $r_e(a^1\Sigma^+) = 1.2769\text{ Å}$.

Correlation consistent,¹⁷ (cc-pVnZ), augmented correlation consistent¹⁸ (aug-cc-pVnZ), and core-valence correlation consistent¹⁹ (cc-pCVnZ) basis sets were used throughout. The largest such basis sets used, cc-pV5Z, is of $[6s5p4d3f2g1h]$ quality. Where appropriate, contributions were extrapolated to the one-particle basis set limit using the $A+B/L^3$ formula of Halkier *et al.*²⁰

III. RESULTS AND DISCUSSION

All computed values are given in Table I, compared with available experimental data.

As expected, the CCSD results are grossly biased towards the triplet state ($T_e = 4432\text{ cm}^{-1}$ at the basis set limit). Inclusion of $\hat{T}_3$ (connected triple excitations) is required for an even qualitatively correct result, although even the

^{a)}Electronic mail: comartin@wicc.weizmann.ac.il

TABLE I. $X^3\Pi-a^1\Sigma^+$ of BN transition energy (cm^{-1}).

	Valence correlation						Best estimate	Running total
	cc-pVDZ	aug-cc-pVDZ	cc-pVTZ	aug-cc-pVTZ ^a	cc-pVQZ	cc-pV5Z		
CCSD	4250.7	4619.8	4375.6	4469.7	4420.7	4427.4	4432.2	...
CCSD(T)	-141.2		-180.7		-175.4	-181.1	-199.9 ^b	...
CCSDT	814.6	1203.0	826.3	931.7	831.6	829.6	827.4	827.4
CCSDTQ-CCSDT	-323.7	-375.3	-466.6	-477.9	-494.2	...	-514.4	313.0
CCSDTQ5-CCSDTQ	-50.6	-53.9	-58.3	...	...	...	-61.2	251.8
CCSDTQ56-CCSDTQ5	-7.6	...	...	...	...	...	-7.6	244.2
FCI-CCSDTQ56	-0.9	...	...	...	...	...	-0.9	243.3
	Inner-shell corr.						Best estimate	Running total
	cc-pCVDZ	cc-pCVTZ	cc-pCVQZ	cc-pCV5Z				
CCSD(T)	-15.2	-15.7	-6.2	+4.8			+16.2	...
CCSDT	-36.0	-52.4					-59.3	184.0
CCSDTQ-CCSDT	-12.1	-21.6					-25.6	158.4
Best estimate, this work								158±40 ^c
Incl. spin orbit ^d								183±40
MRACPF, Martin <i>et al.</i> (Ref. 1)								381±100 ^c
MRDCI, Mawhinney <i>et al.</i> (Ref. 2)								241±160 ^c
ICMRCI, Peterson (Ref. 5)								190±100 ^c
ICMRCI, BP (Ref. 6)								180±110 ^c
QMC, Lu (Ref. 12)								178±83 ^c
Expt. (matrix) (Ref. 13)								15–182
Expt. (gas phase) (Ref. 14)								158±36 ^c

^acc-pVTZ basis set used on boron.^bExtrapolated from CCSD(T)/cc-pV5Z value and -189.1 cm^{-1} at the CCSD(T)/cc-pV6Z level.^cValue does not include spin-orbit splitting in triplet state.^dExpt. $A_0 = -25.14 \text{ cm}^{-1}$ (Ref. 22); Calc. $A_e = -24.3 \text{ cm}^{-1}$ (this work).^eFrom observed $T_0 = 0.031 \pm 0.004 \text{ eV}$ (Ref. 14) and ZPVE difference from Ref. 13, assuming 4 cm^{-1} uncertainty on ZPVE difference.

CCSDT basis set limit $T_e = 827 \text{ cm}^{-1}$ is three to four times too large. Quasiperturbative $\hat{T}_3$ corrections such as CCSD(T) overcorrect and wrongly predict a singlet ground state.¹ We conclude that CCSDT is the lowest acceptable level of theory for the reference geometry. Comparison of the CCSDT/cc-pVQZ and CCSDT/cc-pV5Z values suggests that the latter is converged to within 2–3 cm^{-1} with respect to the basis set.

Inclusion of $\hat{T}_4$ (connected quadruple excitations) proved essential for anything approaching quantitative accuracy. The CCSDTQ/cc-pVQZ basis set calculations reported here involve $(419 \text{ and } 391) \times 10^6$ amplitudes, respectively, for the singlet and triplet states. They ran for two weeks each on single AMD Opteron 846 processors. At the basis set limit, $\hat{T}_4$ reduces the transition energy by 514 cm^{-1} . We do note—as we have previously noted⁹ for other strongly multireference systems such as $\text{C}_2(X^1\Sigma_g^+)$ —that basis set convergence for the $\hat{T}_4$ contribution is fairly slow (unlike for systems dominated by a single-reference determinant⁹). This can be rationalized in terms of very prominent double excitations in the singlet wave function: dynamical correlation relative to them will be dominated by double excitations, which represent quadruple excitations relative to the reference determinant. At the CCSDTQ basis set limit, we obtain $T_e = 313 \text{ cm}^{-1}$, in agreement with Ref. 1 but still considerably higher than the other results.

Connected quintuple excitations ($\hat{T}_5$) still reduce the ex-

citation energy by about 70 cm^{-1} . Comparison of the cc-pVDZ and cc-pVTZ results for this contribution suggests that it converges quite rapidly with the basis set.

Connected sextuple excitations only affect T_e by -8 cm^{-1} , while the contribution of still higher excitations was found to be negligible. Our best estimate for the valence-only full configuration interaction (FCI) basis set limit is therefore $T_e = 243 \pm 28 \text{ cm}^{-1}$, where our error bar is the sum of all the amounts covered by extrapolations.

Somewhat surprisingly, the effect of core-valence correlation is found to account for the discrepancy with earlier theoretical studies and experiment. At the CCSDT level, it lowers T_e by $59 \pm 7 \text{ cm}^{-1}$, while the differential $\hat{T}_4$ core-valence contribution reduces T_e by an additional $26 \pm 4 \text{ cm}^{-1}$ at the CCSDTQ level. [The all-electron CCSDTQ/cc-pCVTZ calculations, at 1×10^9 amplitudes each, took about one day per iteration running OPENMP parallel on four AMD Opteron 846 CPUs. Submicrohartree convergence requires about 20 iterations. Our attempts to carry out CCSDT/cc-pCVQZ calculations met with failure for the triplet state. Because of the clearly erratic basis set convergence behavior of the CCSD(T) energy in this case, we have chosen not to use the larger basis set data at this level of theory.]

Our final best estimate neglecting spin-orbit splitting thus becomes $T_e = 158 \pm 40 \text{ cm}^{-1}$, in excellent agreement with the earlier calculations (which likewise neglect spin-orbit splitting, it being almost an order of magnitude smaller than

their stated uncertainties). Our error bar is probably somewhat conservative, as it assumes that no cancellation at all would occur between extrapolation errors in individual contributions.

The spin-orbit coupling constant of the $X^3\Pi$ state is calculated as -24.27 cm^{-1} at the CISD/cc-pVQZ (uncontracted, no g functions) level using MOLPRO,²¹ in excellent agreement with the experimental value²² of -25.14 cm^{-1} . Its inclusion pushes up both the present calculated value and all the earlier theoretical values by these amounts: our final best estimate thus becomes $T_e=183\pm40\text{ cm}^{-1}$. This agrees with the experimental value of Asmis *et al.*¹⁴ to within the respective uncertainties and finds itself near the upper edge of the interval given by Lorenz *et al.*¹³

Finally, as a by-product of this study, we obtain the dissociation energy of $\text{BN}(X^3\Pi)$ using W4 theory²³ as $D_e=105.74\pm0.16\text{ kcal/mol}$ and $D_0=103.57\pm0.16\text{ kcal/mol}$ (the uncertainty being a 95% confidence interval). This is somewhat higher than previous calculated D_e values of 105.2 kcal/mol (Ref. 1) and 104.2 kcal/mol .⁵ The zero-point vibrational energy (ZPVE) of 2.17 kcal/mol was obtained by combining the accurate ω_e and $\omega_e x_e$ for the singlet state from Ref. 24 with the state difference in ZPVE from Ref. 13. In Ref. 23, %TAE[(T)], the percentage of the total atomization energy resulting from (T), was proposed as an indicator for the importance of nondynamical correlation effects. We note that %TAE[(T)]=6.03% for the $X^3\Pi$ state (on the low end of moderate nondynamical correlation), compared to no less than 18.63% for the $a^1\Sigma^+$ state (among the most severe cases surveyed in Ref. 23).

IV. CONCLUSIONS

Summing up, the notoriously small $X^3\Pi-a^1\Sigma^+$ excitation energy of the BN diatomic has been calculated using high-order coupled cluster methods. Convergence has been established in both the one-particle basis set and the coupled cluster expansion. Explicit inclusion of connected quadruple excitations $\hat{T}_4$ is required for even semiquantitative agreement with the limit value, while connected quintuple excitations $\hat{T}_5$ still have an effect of about 60 cm^{-1} . Still higher excitations only account for about 10 cm^{-1} . Inclusion of inner-shell correlation further reduces T_e by about 60 cm^{-1} at the CCSDT, and 85 cm^{-1} at the CCSDTQ level. Our best estimate, $T_e=183\pm40\text{ cm}^{-1}$, is in excellent agreement with earlier calculations and experiment, albeit with a smaller (and conservative) uncertainty. The dissociation energy of $\text{BN}(X^3\Pi)$ is $D_e=105.74\pm0.16\text{ kcal/mol}$ and $D_0=103.57\pm0.16\text{ kcal/mol}$.

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