The Mechanical Properties of Polyvinyl Butyral (PVB) at High Strain Rates

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Abstract

Polyvinyl Butyral (PVB) has been largely used as an interlayer material for laminated glass to mitigate the hazard from shattered glass fragments, due to its excellent ductility and adhesive property with glass pane. With increasing threats from terrorist bombing and debris impact, the application of PVB laminated safety glass has been extended from quasi-static loading to impact and blast loading regimes, which has led to the requirement for a better understanding of PVB material properties at high strain rates. In this study, the mechanical properties of PVB are investigated experimentally over a wide range of strain rates. Firstly, quasi-static tensile tests is performed using conventional hydraulic machine at strain rates of 0.008~0.317s⁻¹. Then high-speed tensile test is carried out using a high-speed servo-hydraulic testing machine at strain rates from 8.7s⁻¹ to 1360s⁻¹. It is found that under quasi-static tensile loading, PVB behaves as a hyperelastic material and material property is influenced by loading rate. Under dynamic loading the response of PVB is characterized by a time-dependent nonlinear elastic behavior. The ductility of PVB reduces as strain rate increases. The testing results are consistent with available testing data on PVB material at various strain rates. Analysis is made on the testing data to form strain-rate dependent stress-strain curves of PVB under tension.

Keywords: PVB; dynamic material property; high-speed tensile tests.
1. Introduction

PVB, short for Polyvinyl Butyral, is a polymer material with outstanding mechanical properties and excellent optical clarity, which has been primarily used as an interlayer material for laminated glass in the field of construction and automobiles. In the manufacture of laminated glass, normally two glass panes are bonded by a transparent polymer interlayer. Due to the low shear stiffness, before glass crack the composite pane carries lateral loads mainly through the two glass plies (Figure 1a). After glass breaks, the interlayer comes into effect. It holds the shattered glass splinters together and prevents them from flying into the occupied area. Post-glass breakage, the glass ply only bears the compressive force, while the PVB interlayer bridging between the shattered glass fragments carries the tensile force (Figure 1b). Although analysis and design of laminated glass against conventional quasi-static and low-rate dynamic loading such as wind is well developed, the behavior of a laminated pane under high-rate dynamic loading such as blast and impact is relatively less understood. Despite many researches onto the response of laminated pane under such loadings being reported recently [1-4], the mechanical behavior of PVB interlayer at high-strain rates still needs be investigated for better predictions of the laminated glass window responses subjected to blast and impact loads.

The mechanical behavior of PVB has been proven to be complicated. It is highly nonlinear, time-dependent, and being capable of undergoing substantial extension. The compressive behavior of PVB under quasi-static and dynamic loadings was exclusively studied [5, 6]. The stress-strain curves at strain rates from $4 \times 10^{-4} \text{s}^{-1}$ to $4 \times 10^{-2} \text{s}^{-1}$ for quasi-static state and at strain rates from $700 \text{s}^{-1}$ to $4500 \text{s}^{-1}$ were obtained using conventional testing machine and Split Hopkinson Pressure Bar (SHPB) technique, respectively. Time-dependent viscoelastic characteristics were observed for PVB under impact. A two-stage behavior, i.e. ‘compaction stage’ and ‘hardening stage’, was introduced to describe the response of PVB under dynamic compression. Through comparison with Ogden model, it was found that Mooney-Rivlin model well describes PVB compressive behavior [5].

The behavior of PVB under tension is more to the interest of studying PVB laminated glass windows, as PVB interlayer is quite thin and only takes tensile force in the composite. The small-strain behavior of PVB has been investigated intensively to analyze the pre-glass crack response of laminated pane under quasi-static loading such as wind pressure. A viscoelastic model is generally introduced for PVB material with a generalized Maxwell series to account for the time-dependent shear modulus [7, 8]. Dynamic mechanical analysis found
that PVB has a rubbery modulus of the order of 1MPa and a glassy tensile modulus in the order of 1GPa [9]. The influence of temperature variation is considered by using the Williams-Landel-Ferry equation to shift the shear modulus of different temperatures. Transition between a rubbery material to a glass-like material occurs at a temperature of 5°C to 40°C [9].

The mechanical behavior of PVB at large strain has been studied through laboratory testing at both the quasi-static and dynamic states. For the quasi-static region, Iwasaki et al. [10] tested 0.76mm thick PVB specimen and derived stress-strain curves at strain rates from 0.0067s^{-1} to 0.2s^{-1}. Bennison et al. [11] obtained stress-strain curves of PVB at strain rate 0.07s^{-1} and 0.7s^{-1}. Liu et al. [6] investigated PVB tensile properties at strain rates of 0.004s^{-1}, 0.02s^{-1}, 0.04s^{-1}, and 0.08s^{-1}. The above tests all found that PVB shows viscoelastic material property under low-speed tension, and the response is influenced by loading speed. Dynamic tensile tests found the dynamic profile of PVB differs significantly from its quasi-static behavior. Iwasaki et al. [10] presented the stress-strain curve of PVB at a strain rate of 118s^{-1}. It depicts that under dynamic loading PVB exhibits elasto-plastic material property with a steep initial rise in stress followed by a decrease in stress increment. A few dynamic tensile tests have been reported lately on PVB material at various strain rates. For instance, using a servo-hydraulic testing machine Bennison et al. [11] tested PVB tensile strength at strain rates of 8s^{-1} and 89s^{-1}. With an Imateck impact test machine, Morison [12] carried out drop weight tests and obtained PVB tensile profile at strain rates from 33.5s^{-1} to 278s^{-1}. Hooper et al. [9] also reported their testing data on PVB at strain rates from 2s^{-1} up to 400s^{-1}. The dynamic testing results found PVB tensile response is characterized with time-dependence. The initial modulus, yield stress, and failure stress will be amplified at increased strain rates. However, as strain rate increases PVB becomes less ductile with diminishing failure strain. The influence of temperature has also been investigated. Morison extended his drop weight tests on PVB at room temperature to another two temperatures, i.e. 5°C and 35°C. It was found that at room temperature despite PVB exhibits elasto-plastic behavior which is analogous to yield in metal, the response remains viscoelastic as the additional deformation in the specimen is gradually recoverable once unloaded. At lower temperature, PVB still behaves elasto-plastically but associated with smaller hardening stiffness. At elevated temperature, the stress-strain curve is much closer to linear viscoelastic.
With more and more applications of PVB laminated glass into retrofits against shock and impact loading where the strain rate that material experiences is high, a thorough investigation of PVB mechanical properties at a wider strain rate range, especially at high-strain rates beyond the current available testing data is needed. In this study, we carry out uniaxial tensile tests on PVB material at a wide range of strain rates. Firstly, low-speed tensile test is performed on 0.76mm thick PVB specimen to investigate its quasi-static behavior at strain rates of 0.008s\(^{-1}\) to 0.317s\(^{-1}\). Then, high-speed tensile test is carried out using a high-speed servo-hydraulic testing machine to study PVB dynamic response at strain rates from 8.6s\(^{-1}\) to 1360s\(^{-1}\). The testing data are analyzed. They are used together with previous testing results obtained by other researchers on PVB to derive a strain-rate-dependent stress-strain relationship for PVB.

### 2. Theory and Methodology

#### 2.1 Testing systems

Experimental techniques commonly used to determine material tensile properties at different strain rates include conventional screw driven load frame, servo-hydraulic machine, pendulum or drop weight impact system, high-speed servo-hydraulic machine, and Split-Hopkinson Pressure Bar system. The conventional testing systems including the screw driven load frame and conventional servo-hydraulic machine can normally test material tensile strength at a strain rate up to 1s\(^{-1}\). Split-Hopkinson Pressure Bar (SHPB) is commonly used to determine material strength at high strain rates (\(\dot{\varepsilon} \geq 100s^{-1}\)). In determining the material tensile properties, the tensile SHPB usually requires the testing specimen to be firmly glued on both ends respectively to the incident and transmitter bars to ensure the tensile stress wave can travel through the specimen before it fractures. It is therefore not ideal to test polymer materials like PVB, as the glue could significantly alter material properties. The pendulum or drop weight impact system and the high-speed servo-hydraulic machine have been widely used to determine material strength at strain rate above 1s\(^{-1}\). Dog-bond shaped specimens similar to those used for quasi-static tests are most commonly adopted for the dynamic tensile tests. Due to inherit difficulties, the strain rates that can be achieved by a drop weight impact machine is usually limited to below 100s\(^{-1}\). Moreover, during a test the velocity of the actuator is interacted with the response of the specimen. It is difficult for the drop weigh impacter to maintain a constant velocity. In this study, servo-hydraulic and high-speed servo-hydraulic machines are used to perform the low-speed and high-speed tensile
tests. The testing setups and machine information are described in details in section three and four.

2.2 Testing requirements for high-speed tests

To ensure the validity of testing data for a material test, it is critical to assure the specimen is under the state of stress equilibrium. For low-speed tests, the specimens are in quasi-static equilibrium as comparing with the loading duration there is more than sufficient time for elastic wave to travel back and forth many times inside the specimen. For high-speed tests, to achieve the state of stress equilibrium is much more difficult since the loading time can be much shorter. In a dynamic test, a state of dynamic equilibrium is usually pursued, where a minimum number of elastic waves are required to propagate through the specimen. To estimate the time for one stress wave to travel a round trip in the specimen the following relation can be utilized

\[ t = \frac{2L}{c} \]  

where \( L \) is the specimen length between the clamping grips; and \( c \) is the elastic stress wave velocity in the testing material. The one-dimensional longitudinal wave velocity in an isotropic material can be estimated by the relation

\[ c = \sqrt{\frac{E}{\rho}} \]  

where \( \rho \) is the density of the material, and \( E \) is the Young’s modulus.

To reach dynamic stress equilibrium, a SHPB test normally requires at least three reverberations of the loading wave in the specimen [13, 14]. Based on dynamic tensile tests using a high-speed servo-hydraulic machine on different plastic materials, it has been found the criterion for a valid SHPB test is also applicable to dynamic direct tensile test [15]. The draft standard of the Society of Automotive Engineers on high strain-rate tensile test for automotive plastics requires at least 10 elastic reflected waves propagating through the specimen from the time of loading to the time of yield. There is no quantitative criterion in the open literature yet defining the exact number of reflected stress wave in the specimen to achieve dynamic equilibrium for a uniaxial tensile test.
3. Low-Speed Tests

3.1 Test setup

PVB specimens for the low-speed tests were made from 0.76mm thick PVB sheets using the punch as shown in Figure 2. The specimen is in a dog-bone shape with a central testing gauge of 40mm in length. Plastic tabs are attached to the tails of the specimen to ensure the thin PVB film will not slip from the clamping jaw. It is worth noting that due to the very low thickness of the specimen, in the preliminary testing even with the added plastic tabs the specimen would still slip. Worse still, any fixing glue applied directly onto the PVB specimen would alter the material property and make it brittle. After some trials, an additional layer of soft cloth (as shown in Figure 2) is introduced between the plastic tab and specimen. Satisfactory clamping was achieved in this manner and good testing results were obtained.

The low-speed test was performed in two stages. In the first stage, uniaxial tensile test was carried out on a Baldwin universal testing system with additional clamping device to fix the specimens, and an external load cell to measure the applied force (Figure 3a). The Baldwin machine is a servo-hydraulic system where the actuator velocity is controlled manually with applied oil pressure. 8 PVB specimens were tested on this machine with measured strain rates varying from 0.008s\(^{-1}\) to 0.043s\(^{-1}\). In the second stage, an Instron hydraulic testing machine UTS-5982 as shown in Figure 3b is utilized. The actuator of the machine can maintain a computer controlled constant pulling speed of 50mm/min to 1016mm/min with a maximum stroke length of 1430mm. The applied force and the deformation of the PVB specimen were monitored using an inbuilt load cell and extensometer on top of the upper clamp. Another 15 specimens were tested on the Instron machine at four crosshead velocities, i.e. 50mm/min, 250mm/min, 500mm/min, and 800mm/min, corresponding to nominal strain rates of 0.0198s\(^{-1}\), 0.0992s\(^{-1}\), 0.1984s\(^{-1}\), and 0.3175s\(^{-1}\). The room temperature during the test was around 23°C±5°C.

3.2 Results

The machine crosshead displacement is used to evaluate the elongation of the specimen. Specimen strain is determined by using the elongation dividing its original length. The strain rate that specimen experienced is derived by differentiating strain time history. Figure 4 shows a sample strain-rate time history derived from the machine crosshead displacement (specimen G04). As can be observed, the machine quickly reaches the designed testing velocity and the specimen is pulled at a constant velocity until the specimen fractured as indicated. Engineering stress-strain curves obtained from the low-speed tensile tests are
shown in Figure 5. As shown, under low-speed tension PVB displays viscoelastic property. The stress increases with strain in an exponential form. The stress increases gradually with the strain in the beginning, and then grows steeper as strain increases. The behavior of PVB under low-speed tensile loading shows strain-rate dependence. As show in Figure 5, the inclination of the stress-strain curves becomes steep as the tensile speed increases. The failure strains of PVB at low-speed test are generally over 200%. But as pulling speed increases, PVB becomes brittle and the failure strains become smaller. For instance, when the strain rate was 0.02s\(^{-1}\), the specimen failed with an ultimate strain of 245%. As strain rate increased to 0.317s\(^{-1}\), the failure strain dropped to 175%. The testing results on PVB specimen under low-speed tension are summarized in Table 1. It should be noted that because of the non-uniform elongation of material around the shoulders of the specimen, the strain derived using machine crosshead displacement could introduce some deviation. But since the length of the shoulder is relatively short comparing with the entire length of the specimen, the deviation is believed to be small.

4. High-Speed Dynamic Tests

The high-speed tensile test was carried out at the Tianjin University and Curtin University Joint Research Center. The room temperature during the test was about 30°C±3°C. A high-speed servo-hydraulic test machine was utilized with an actuator pulling speeds ranging from 0.1m/s to 20m/s. The tests discovered the dynamic material properties of PVB at strain rates ranging from approximately 8.6s\(^{-1}\) to 1360s\(^{-1}\).

4.1 Test setup

An Intron VHS testing system (VHS 160-20) is utilized to carry out the high-speed test. The machine is comprised of a fast jaw grip which accelerates upwards in the direction of tension (Figure 6a). As soon as the jaw reaches the designed testing velocity, a wedge will be knocked out to release the sprung grip to grab the upper clamping bar and pull it up at the designed testing velocity till failure. The actuator of the machine can maintain a constant velocity from 1mm/s to 1m/s under closed loop control, and a maximum velocity of 25m/s under open loop control. Specially designed lightweight clamps as shown in Figure 6b are designed and made to fix the specimens. The upper clamp comprises of a 350mm long arm which is riveted to a 60mm by 60mm alloy tab. The fast jaw travels freely along this arm and grab it when it reaches the designed testing velocity. 4 plastic bolts are used to fasten another alloy tab to clamp the tail of the PVB specimen firmly. The lower clamp has the same structure but with a shorter alloy arm to be fixed into the bottom grip head. The
clamps are made of magnesium alloy (AZ31B). The density of the alloy is 1770kg/m³. To minimize the influence of inertia effect, the clamps are only 1mm thick. The yield strength of alloy is about 200MPa under uniaxial tension, and the Young’s modulus is 44.8GPa. The high strength and large modulus compared to those of PVB assure the clamping bars will not yield nor result in large elongation during the test.

The PVB specimens for the high-speed tensile tests were sampled from 0.76mm PVB sheet used for laminated glass. Due to the low strength of the material, eight layers of 0.76mm PVB sheets were stacked together, heated to about 70°C and then pressed by a roller to squeeze out the air or any blister. The process follows the manufacture procedure of producing laminated glass panes. In such a manner, 6.08mm±0.05mm thick PVB sheets were made. Using a die cut, the 6.08mm thick PVB sheets were machined into the geometry as shown in Figure 7. The 10mm central testing gauge was marked with thin black lines with a permanent marker to enable optical strain measurement with high-speed camera. The dog-bone shape specimen has two long tails to be clamped by the alloy tabs. To avoid slippage of specimen being pulled out of the clamping tabs, two additional plastic tabs were added to the tails of the PVB specimens.

A linear variable differential transducer (LVDT) embedded in the fast jaw was used to track the movement of the actuator. A one-dimensional accelerometer mounted on the fast jaw was used to monitor the acceleration. A piezo load cell fixed below the bottom grip was utilized to measure the force transmitted. The signals of these transducers were connected to a data acquisition system with a sampling frequency of 65kHz. The deformation process of the PVB specimen was monitored by a high-speed camera (Photron® Fastcam SA 1.1). The aperture of the lens was set to its widest opening, which is balanced with the exposure time. A 2000w halogen light M-300G by Leiying® was used to provide lighting (Figure 6a). The frame rate was set to 1000~8000fps restricted by the testing speed and camera cache. The camera was synchronized with a TTL pulse from the Instron testing system. High-speed camera images were post-processed with an image tracking algorithm. The relative displacement time histories at the two black marking lines were used to determine the elongation of the specimen at its central testing region. The engineering strain was then calculated using the elongation divided by the original gauge length. The strain rate that each specimen experienced was derived through differentiating the strain history.

4.2 Results

High-speed tensile testing results on PVB material are presented in this section. An example of the test on PVB specimen (F07) with an actuator speed of 1m/s is shown to demonstrate
the specimen’s deformation-to-failure process, and the strain rate history derived from high-speed camera images. The load time history and the way how inertia force is deducted is demonstrated. Validation of dynamic equilibrium for high-speed tensile test is carried out. Then, the testing results of all the PVB specimens are presented.

4.2.1 Failure process

The deformation-to-failure process of specimen F07 is shown in Figure 8. All the images have been flipped from vertical to horizontal direction and stacked for demonstration convenience. At t=0ms the actuator was accelerating towards the designed testing velocity. The specimen was at rest as the fast jaw was not in contact yet. At t=11ms, the PVB specimen began to be stretched. The specimen deformed quickly under the tensile force. As can be observed, due to the substantial deformation of the specimen, even the two thin black reference markers were stretched. At t=111ms, the specimen experienced great elongation. Fracture initiated from its centre which splitted the specimen into halves. The machine came to a rest after the specimen broke.

The high-speed camera images were post-processed. The displacement trajectories at the two black markers were traced and used to form the specimen elongation history at its central testing gauge. The strain was derived by using the elongation divided by its original length between the two markers, and the strain rate history is calculated by differentiating the strain time history. As shown in Figure 9, the strain rate rises quickly to about 60s\(^{-1}\) after the fast jaw gripped the clamping bar. A plateau is formed as the specimen was pulled at a constant 1m/s velocity. The specimen elongates at a relatively constant strain rate of 60s\(^{-1}\) until fracture occurs which is indicated on the strain rate history when it suddenly ascends due to the rebound of deformed specimen. The measured strain rate is a lot lower than the nominal strain rate (\(\dot{\varepsilon}_{\text{nom}} \approx 100s^{-1}\), estimated with the actuator velocity 1m/s dividing the testing gauge length of 10mm). This is because of deformation of PVB material at the shoulders of the tested specimen.

4.2.2 Load time history

The load time history recorded by the load cell for specimen F07 is shown in Figure 10. The inertia force (\(F_{\text{inertia}}\)) from the clamping devices is calculated by using the mass of clamps \(m_{\text{clamp}}\) including both the alloy bars and the bolts times the recorded acceleration from the accelerometer (a). The calculated inertia force is deduced from the total force \(F_{\text{total}}\) to derive the net force \(F_{\text{net}}\) experienced by the PVB specimen.

\[
F_{\text{inertia}} = m_{\text{clamp}} \times a
\]
\[ F_{\text{net}} = F_{\text{total}} - F_{\text{inertia}} \]

As shown in Figure 10, the contribution of inertia force is negligible because of the light weight of the specially designed clamping device. In this way, the influence of inertia from the clamping devices is deducted, and the pure PVB material response is obtained for the high-speed test.

4.2.3 Validation of high-speed test

In high-rate test the condition of dynamic stress equilibrium should be properly checked to ensure the validity of testing data. For high-speed test a sudden applied impulse can excite “system ringing”, which causes high amplitude stress oscillation and non-homogeneous deformation in the specimen [15]. It is therefore important to ensure stress wave travel in round trips for a sufficient number of times in the specimen to achieve stress uniformity in the specimen. The wave speed in the PVB specimen can be estimated using Eq. (2). For the PVB material with Young’s modulus 190MPa and density 1.07g/cm³, the wave speed in the specimen is about 421m/s. For a 20mm testing gauge length (between clamps) it takes about 47μs for the stress wave to propagate through the specimen. For the above specimen F07, the stress wave can propagate through the specimen for 78 times in round trips before it reaches the yielding point (according to load time history it takes about 7.32ms), and about 1290 times before the specimen fractures (it takes about 121.29ms), which is more than sufficient to achieve stress equilibrium. Even at the maximum actuator pulling velocity of 20m/s performed in the present tests, it still takes about 0.21ms before it reached the yielding point, and about 4.11ms before the specimen fractures. The stress wave could travel within the specimen for more than twice before PVB yields, and about 44 times round trips before the specimen fractures. It is therefore confident that the condition of stress equilibrium is satisfied in the high-speed tensile tests for the current study, and the testing results measured are valid.

To ensure valid testing results are obtained from the dynamic test, the response of the testing system should also be carefully checked. If the nature period of the system is not shorter than the rising time of the applied force onto the specimen, the force measured by the load cell will not properly track the real response of the specimen because of interactions. A load time history measured from the system after a specimen suddenly breaks is shown in Figure 11. It can be estimated that the nature oscillation period of the testing system is about 250μs. When the actuator was pulling at a velocity of 1m/s as shown above for specimen F07, the rising time of the tensile force to the point where the specimen initial yielded was approximately 6440μs, which was a lot longer than the nature period of
When the actuator pulling velocity increases to 8 m/s the rising time is about 870 μs. As the actuator velocity approaches the maximum velocity of 20 m/s in the present tests, the rising time for the applied force to reach the yield stress is about twice the nature period of the system, which is the practical limit for the load cell being able to track the material response [9].

4.2.4 Engineering stress versus engineering strain curves

Figure 12 shows the engineering stress vs. strain curves for the PVB specimens in the high-speed tests at actuator speeds varying from 0.1 m/s to 20 m/s. As can be observed, PVB material behaves very differently from that at quasi-static state. The stress shows a steep initial increase until a turning point from where the rise in stress slows down. The stress-strain curve depicts typical elasto-plastic like material property. However, the drop in modulus is not an actual sign that the material has yielded. Almost all the elongation of specimen was recovered after it fractured. Similar observations were also reported by previous researchers [9, 12]. It indicates that despite approximately an elasto-plastic model or a bilinear relationship with strain hardening can be used to describe the behavior of PVB under tension without unloading, the extension in PVB material is viscoelastic rather than plastic. If unloading behavior of PVB is to be considered, a bilinear viscoelastic model is preferable rather than an elasto-plastic model with hardening. It should be noted that due to testing difficulty there has not been any testing data reported in the literature yet on the unloading behavior of PVB at high strain rates. Therefore, the unloading path of PVB after dynamic tensile loading is still not properly understood. In this study, for easy demonstration of PVB mechanical behavior at high strain rate, a pseudo yield stress ($\sigma_{ps,y}$) where material modulus change abruptly, and the corresponding strain - pseudo yield strain ($\varepsilon_{ps,y}$) are defined. The stress at failure $\sigma_f$, and the strain at failure $\varepsilon_f$ are calculated at the time when the specimen fractures. Two modulus are considered, the initial modulus $E_{ini}$ which is defined as the gradient of a secant line through the pseudo yielding point and the origin on the engineering stress-strain curve, and the secondary modulus $E_{sec}$ corresponding to the gradient between the pseudo yielding point and the ultimate failure point on the stress-strain curve. Table 2 summaries these testing results for the high-speed tensile test.

The engineering stress-strain curves for PVB in Figure 12 show that the response of PVB is very strain-rate dependent. When the actuator speed is 0.1 m/s, which corresponds to a strain rate of about 8 s$^{-1}$, the behavior of the PVB is similar to viscoelastic material with large nonlinear deformation till the point of failure. As strain rate increases, the initial modulus increases. The pseudo yield stress also increases with strain rate. When the strain rate
increases from about 8s\(^{-1}\) to over 1300s\(^{-1}\), the initial modulus increases from about 70MPa to 120MPa, and the yield stress rises from about 3MPa to over 16MPa. It can also be observed that PVB material becomes less ductile at increased strain rates. The failure strain reduces from over 200% to 140% when the strain rate increases from 8s\(^{-1}\) to 1300s\(^{-1}\). Oscillation was observed from the stress-strain curves as actuator speed increases above 6m/s, and becomes more apparent with the increase of the actuator speed. This is because of the relatively low strength of PVB material and the vibration of the testing system. The period of oscillation matches with the natural period of the load cell and the clamping device.

5 Analysis and Discussion

The testing results from both the low-speed and high-speed tensile tests are analyzed in the following section. Available testing data reported in the literature [9-12] are also included for the analysis. Discussions are made on the strain rate effect. Empirical formulae are derived from best fitting the testing results. It is worth noting that to be consistent with previous studies, in this section engineering stress and strain are utilized when analyzing the results.

5.1 Strain rate effect

Figure 13 illustrates selected engineering stress-strain curves of PVB at various strain rates. As can be seen, loading speed has very significant influence on the behaviors of PVB material. At a strain rate of 0.019s\(^{-1}\), PVB behaves essentially viscoelastic. As strain rate increases to 0.198s\(^{-1}\), PVB shows similar viscoelastic property but the initial stress rises quickly until a turning point. This phenomenon becomes more apparent when the strain rate increases to 0.317s\(^{-1}\). Under the tensile loading, the initial stress quickly jumps to about 1.5MPa, and the fast increase in stress slows down and then increases in an exponential form with strain. As strain rate further increases, the pseudo yielding point becomes more and more apparent. The corresponding yield stress also increases with the strain rate. As shown after the pseudo yielding point the nonlinear behavior becomes less noticeable. PVB displays a bilinear viscoelastic property. The transition from nonlinear viscoelastic at low strain rate to bilinear viscoelastic is gradual. As strain rate increases, the pseudo yielding point becomes more and more apparent with higher pseudo yield stress at higher strain rate. After the pseudo yielding point the behavior of PVB gradually transforms from exponential viscoelastic to almost linear viscoelastic. As can be seen, the response of PVB specimen at strain rate 7.7s\(^{-1}\) is still quite similar to those tested at low strain rates.
5.2 Pseudo yield stress and yield strain versus strain rate

The pseudo yielding point on the stress-strain curve is important to model the bilinear behavior of PVB material. The pseudo yield stress and strain from the current tests (\(\dot{\varepsilon} \geq 0.198 \text{s}^{-1}\)) together with previous testing data reported in literature are summarized and plotted in Figure 14 and Figure 15 as a function of strain rate. The testing data from the current study show consistency with previous studies. As can be seen, the pseudo yield stress shows a clear trend of increase with strain rate. When the strain rate is about 0.198 \(\text{s}^{-1}\), the yield stress is about 0.5 MPa. As strain rate increases to about 8.6 \(\text{s}^{-1}\), the yield stress is about 4 MPa. As strain rate becomes higher, the increase in the yield stress becomes faster. When the strain rate reaches to 135 \(\text{s}^{-1}\), the yield stress is about 10 MPa. The yield stress rises to about 20 MPa at strain rate 686 \(\text{s}^{-1}\). The increasing yield stress can therefore be approximated by a bilinear trend line as

\[
\sigma_{yield} = 1.689 + 1.573 \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} \leq 10\text{s}^{-1}
\]

\[
\sigma_{yield} = -4.533 + 8.351 \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} > 10\text{s}^{-1}
\]

where \(\sigma_{yield}\) is the pseudo yield stress and \(\dot{\varepsilon}\) is the strain rate. \(\dot{\varepsilon}_0\) is a reference strain rate of 1 \(\text{s}^{-1}\). The constants can be determined through nonlinear regression as presented in Eq. (4).

The pseudo yield strains of the current test fall in the range between 0.04 and 0.10. The yield strain appears to be steady in the tested strain rate range, which is also consistent with Bennison et al.’s testing data [11]. The measured yield strain values from Morison [12] and Hooper et al. [9] vary significantly. This can be attributed to the difficulties when measuring the very soft material PVB at high strain rate, and also the difficulty in properly defining the pseudo yielding point and therefore the yield strain.

5.2 Initial modulus versus strain rate

Figure 16 shows the tested initial modulus, \(E_m\) of PVB material with respected to the strain rate. As can be observed, the initial modulus determined from the current test varies between 7 MPa and 320 MPa, which follows an increasing trend with strain rate. Under tensile loading, the initial modulus is only about 7 MPa at a strain rate of about 0.198 \(\text{s}^{-1}\). The initial modulus increases quickly as strain rate increases. At strain rate 8 \(\text{s}^{-1}\), the modulus is about 30 MPa, which rises to around 110 MPa when strain rate is over 70 \(\text{s}^{-1}\). As strain rate approaches 1000 \(\text{s}^{-1}\), the initial modulus increases to about 300 MPa. As pointed out by
Bennison et al. [11] that by increasing the strain rate PVB shifts from a rubbery material, essentially above its glass transition temperature, to a glassy elasto-plastic like material, essentially below glass transition temperature. Except a couple of points provided by Morison [12], the derived initial modulus in the current work agrees with the other previous testing data. Significant variation can be noted between Morison’s testing results themselves around a strain rate about 35s\(^{-1}\). This is very likely to be resulted from the difficulty involved in conducting high-speed tensile test on very soft material like PVB. These contradictory points are excluded. Through best fitting the testing results, a bilinear expression similar to that for the yield stress can be used to express the initial modulus

\[
E_{\text{ini}} = 25.648 + 11.608\log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} \leq 10s^{-1} \\
E_{\text{ini}} = -92.275 + 129.490\log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} > 10s^{-1}
\]  

(5)

where \(E_{\text{ini}}\) is the initial modulus and \(\dot{\varepsilon}\) is the strain rate. \(\dot{\varepsilon}_0\) is a reference strain rate of 1s\(^{-1}\). The constants in Eq. (5) are determined by nonlinear regression.

5.3 Failure stress and strain versus strain rate

The engineering failure stress and strain include both the low-speed and the high-speed testing data are summarized and plotted in Figure 16 and Figure 17. Quasi-static tensile testing results recently reported by Liu et al. [6] are also included in the analysis for completeness. As shown in Figure 17, the failure stress of the current test shows obvious strain-rate dependency. The failure stress increases from about 24MPa at a strain rate of 0.008s\(^{-1}\) to about 30MPa at a strain rate of 8s\(^{-1}\). The dynamic increment effect becomes more apparent as strain rate increases beyond 10s\(^{-1}\). When PVB material deforms at a strain rate of 1360s\(^{-1}\), the failure stress increases to about 40MPa. The high-speed tensile testing results show good consistency with Iwasaki et al.’s [10], Hooper et al.’s [9] and Bennison et al.’s [11] testing data. Variation in failure stress can be found on Morison’s drop weight tests [12], which vary from about 20MPa to 30MPa at a strain rate of 30s\(^{-1}\). The reason leading to this variation is the interaction between the testing system and the specimen, as a result of which the strain rate that material actually experienced is not as what was estimated. Large variation can also be observed on the low-speed testing results in the current study. The failure stresses of the low-speed tests fall in the range between 20MPa and 35MPa. Despite the variation, an increasing trend can be observed with strain rate. A lot lower failure stresses can be found on Liu et al.’s quasi-static testing results [6]. This is probably because of premature failure of PVB specimens. Considering the above variations, Morison and Liu et
al.’s testing data are not included when data fitting the following empirical formula for failure stress. A two-stage data-fit equation for the failure stress can be expressed as

\[
\sigma_f = 27.961 + 1.7753 \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} \leq 1s^{-1}
\]

\[
\sigma_f = 30.698 + 2.3415 \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \quad \dot{\varepsilon} > 1s^{-1}
\]

(6)

where \( \dot{\varepsilon}_0 \) is a reference strain rate \( \dot{\varepsilon}_0 \) of 1s\(^{-1}\).

The failure strains measured in the current test are consistent with most of previous testing results [6, 9-11] at both the quasi-static and dynamic regions. The results provided by Morison [12] are however lower than the current testing data. This is likely due to the different testing technique utilized to measure the specimen displacement. In his dynamic tensile test, Morison adopts the machine actuator displacement to evaluate the specimen strain. Because of the deformation of specimen at shoulder, the strain at the central testing gauge is greatly underestimated. In contrast, in this study the specimen extension and strain are traced by optical device targeting at the central region of the specimen only. More accurate testing results are believed to be obtained in the current test. As shown in Figure 18, the failure strain decreases with the increased strain rate, indicating PVB material becomes less ductile as pulling speed increases. At a strain rate of about 0.01s\(^{-1}\), failure occurs when strain is nearly 300%. The failure strain reduces to about 220% at a strain rate of 0.2s\(^{-1}\). When the strain rate is above 100s\(^{-1}\), the failure strain reduces to below 200%. At a strain rate of 700s\(^{-1}\), the failure strain plummets to only 150%. An expression of Eq. (7) can be used to approximate the failure strain

\[
\varepsilon_f = \varepsilon_{f0} - m_f \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)
\]

(7)

where \( \varepsilon_f \) and \( \dot{\varepsilon} \) represent the engineering failure strain and strain rate, \( m_f \) is a constant, and \( \varepsilon_{f0} \) is the failure strain at the reference strain rate \( \dot{\varepsilon}_0 \) of 1s\(^{-1}\). Nonlinear regression finds \( \varepsilon_{f0} \) to be 2.198±0.024, and \( m_f = -0.1176±0.013 \).

Figure 19 shows the derived secondary modulus at various strain rates. As shown the values of the secondary modulus vary in the range of 9MPa to 16MPa, and appear to be steady with respect to the strain rate. A slight decrease in secondary modulus with respect to the rise of strain rate can be found after data fitting. The derived secondary modulus is consistent with the scatters from the other researchers [9-12]. It is worth noting that different from the secant secondary modulus we use herein, considering the hyperelastic nonlinear deformation of PVB right from its pseudo yielding point, Hooper et al. [9]
introduce the modulus $E_{20}$ which corresponds to the gradient of the stress-strain curve at 20% strain. As shown in Figure 19, the data of $E_{20}$ from Hooper et al. is lower than the plastic modulus we defined above. Excluding the data of $E_{20}$, the testing data are fitted to form the empirical formula of the plastic modulus of PVB as

$$E_{sec} = E_0 + m_e \log_{10} \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)$$

where $E_{sec}$ and $\dot{\varepsilon}$ stand for the secondary modulus and strain rate; $m_e$ is a constant and $E_0$ is the secondary modulus at the reference strain rate $\dot{\varepsilon}_0$ of 1s$^{-1}$. The constants were determined using nonlinear regression and were found to be $E_0=13.971$MPa±0.399MPa, and $m_e=0.432$MPa±0.223MPa.

6 Conclusion

In this paper we present laboratory tests to study the dynamic material properties of polymer material PVB. Low-speed and high-speed uniaxial tensile tests were carried out on PVB specimens covering a wide strain rate range from 0.008s$^{-1}$ to 1360s$^{-1}$. The engineering stress-strain curves obtained show that PVB exhibits viscoelastic material property under quasi-static loading. As strain rate increases, it transfers into a bilinear viscoelastic material which appears to be similar to elasto-plastic material. The pseudo yield stress increases with strain rate from about 3MPa at a strain rate of 8s$^{-1}$ to nearly 20MPa at a strain rate of 1360s$^{-1}$. As strain rate increases no significant increment was found on the corresponding yield strain. The increase in yield stress was mainly attributed to increment in initial modulus. It was also found that the engineering stress to failure varied from 24MPa at a strain rate of 0.008s$^{-1}$ to about 40MPa at 1360s$^{-1}$. The failure strain was found to vary between 280% at 0.008s$^{-1}$ to about 140% at a strain rate of 1360s$^{-1}$ showing a decreasing trend over the tested strain rate range. The secondary modulus of PVB material for the dynamic test was found insensitive to strain rate, which vary in the range of 9MPa and 16MPa. The current testing results were analysed together with previous testing data on PVB. Empirical formulae are derived through best fitting the testing data.

Acknowledgement

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for providing testing materials. The first author would like to acknowledge the Ad Hoc scholarship from the University of Western Australia.

Reference

1. Table 1 Summary of low-speed testing results

2. Table 2 Summary of high-speed tensile testing results

18
<table>
<thead>
<tr>
<th>Specimen No.</th>
<th>Testing machine</th>
<th>Engineering strain rate (s(^{-1}))</th>
<th>Engineering failures strain</th>
<th>Engineering failure stress (MPa)</th>
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Table 1 Summary of low-speed testing results
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<th>Engineering (\varepsilon_{p.s,y})</th>
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<th>Engineering (\sigma_{f}) MPa</th>
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Figure 18 Engineering failure strain vs strain rate
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a) Pre-glass ply breakage  
b) Post-glass ply breakage

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Specimen fractured.
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