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Predicting the peak resistance of a spudcan penetrating sand overlying clay

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Predicting the peak resistance of a spudcan penetrating sand overlying clay

Abstract

Accurately predicting the peak penetration resistance, $q_{\text{peak}}$, during spudcan installation into sand overlying clay is crucial to an offshore mobile jack-up industry still suffering regular punch-through failures. This paper describes a series of spudcan penetration tests performed on medium loose sand overlying clay and compares the response to existing centrifuge data from tests performed on dense sand overlying clay. Together this data demonstrates that punch-through is a potential problem for both dense and loose sand overlying clay soil stratigraphies. Using this experimental database the failure stress dependent model of Lee et al. (2009) has been modified to account for the embedment depth and the depth of occurrence of $q_{\text{peak}}$ is shown to be a function of the sand thickness, $H_s$. The model has then been recalibrated, taking these findings into account, for a larger range of material properties and ratios of sand thickness to spudcan diameter ($H_s/D$). Finally, the performance of the modified and recalibrated model is verified by comparing its predictions to those calculated using the current recommended practice given in the ISO (2012) ‘guidelines’. The comparisons show that the modified model yields more accurate predictions of $q_{\text{peak}}$ over the range of $H_s/D$ of practical interest, which when used in practice will potentially mitigate the risk of unexpected punch-through on sand overlying clay stratigraphies.

CE Database subject headings:

Centrifuge models; load bearing capacity; sand; clays; footings; offshore structures

Keywords:

Centrifuge modelling; spudcan; sand; clay; punch-through; offshore engineering
Introduction

Modern jack-up structures typically consist of a triangular platform with three legs that are jacked through the deck into the seabed. A jack-up is then installed by filling water ballast tanks on the platform, which pushes the legs and large inverted conical spudcan footings attached at the ends into the seabed soil. This preloading procedure continues until the spudcans have been effectively proof tested, at which time the ballast water is dumped and the platform is jacked up above the water surface for operation. When jack-up platforms are installed on seabed sediments consisting of a sand layer overlying soft clay, there is the potential for punch-through failure, where the spudcan footing pushes the stronger layer into the softer layer. This can cause vertical displacement of one or more legs of the platform in a rapid and uncontrolled manner, which as a consequence can lead to buckling of the legs or in extreme cases even toppling of the platform. The cost of these incidents is estimated at between US$10-30 million and they are continuing to be problematic (Hossain and Safinus, 2012). Therefore, accurately predicting the peak penetration resistance and thus the potential for punch-through failure is an important issue for jack-up platform operators both for operational safety and field development economics.

Craig and Chua (1990) performed a series of centrifuge tests investigating the potential for punch-through of foundations on sand overlying clay. They observed that a peak penetration resistance was attained relatively rapidly, which was followed by reducing penetration resistance that caused rapid leg penetration. Cutting of the samples along the central cross section after spudcan extraction exposed a slightly downwards-tapering plug of sand with depth approximately equal to the sand layer height. In contrast, an inverted truncated cone sand plug was visualized by Teh et al. (2008) using the particle image velocimetry technique (White et al. 2003) in a centrifuge and the failure mechanism of spudcan foundations on sand overlying clay was discussed. Teh et al. (2010) proposed that the bearing resistance–depth profile of a punch-through event can be determined by three characteristic bearing resistances and corresponding depths. Based on an extensive series of flat footing and spudcan penetration tests on dense sand overlying clay and the observations of Teh et al. (2008), Lee et al.
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(2009) proposed a failure stress dependent model to calculate the peak penetration resistance, $q_{peak}$. However, the model was calibrated solely using experimental data for dense sand overlying clay and for limited geometries of spudcan foundations. Its performance, therefore, requires further validation. Of greatest concern is whether re-calibration is needed for looser sands overlying clay soil conditions.

The aims of this paper are to:

1. Model experimentally the penetration resistance of a spudcan of generalized geometry penetrating medium loose sand overlying clay in the centrifuge, and access the potential for punch-through failure.

2. Extend the stress dependent model for predicting peak penetration resistance of Lee (2009) to (i) both loose and dense sands and (ii) to account for the embedment depth of the peak penetration resistance.

3. Recalibrate the modified model based on the experimental results.

4. Investigate the ability of the modified model to predict peak penetration resistance during spudcan foundation installation on sands overlying clay.

5. Assess the performance of the modified model by comparison with current recommended practices using centrifuge data reported in the literature.

**Experimental Setup**

Physical modelling of spudcan penetration on medium loose sand overlying clay was conducted using the drum centrifuge at the University of Western Australia (UWA), a detailed description of which was reported by Stewart et al. (1998). Spudcan foundations in practice are typically circular with diameters of 10 to 20 m. In this investigation a generalised geometry spudcan as illustrated in Fig. 1, was used and referred to as the UWA spudcan. The spigot angle of 76° and main conical angle of 13° were kept constant for different model spudcan diameters to ensure any geometric impacts remained consistent between tests. Table 1 contains a summary of the prototype spudcan geometries tested in
this investigation. This UWA spudcan was identical to the model spudcan in dense sand overlying clay by Lee (2009).

Commercially available super fine silica sand and kaolin clay were adopted in all the centrifuge tests to form the sand and clay layers respectively. Both materials have been well characterized and used extensively in the geotechnical centrifuges at UWA. The key properties of the sand and clay are summarized in Cheong (2002) and Stewart (1992) respectively.

The kaolin clay was mixed into slurry with a water content of 120%. It was then placed in the drum channel using the actuator at an acceleration of 20 g until the channel was full, before being normally consolidated at an acceleration of 300 g. After consolidation, the normally consolidated clay was scraped back leaving a non-zero shear strength at the sample surface and the desired target clay thickness of 150 mm. A fabric membrane was then placed on top of the clay, and sand was pluviated into the channel under an acceleration of 20 g using a specially-designed sand placement tool. Medium loose sand was formed by pluviating the fine particles through a layer of water kept on top of the sample. The underlying clay was then lightly over-consolidated at an acceleration of 300 g. The sand and fabric membrane were then removed before the sand was laid again following the same procedure but without the fabric membrane. The fabric membrane was used to facilitate removal of the surcharging sand layer, which was disturbed during normal consolidation of the underlying clay layer, allowing relaying of a new undisturbed sand layer for testing. A target sand thickness was achieved by scraping the sand surface down to the desired height by means of a scraping plate attached to the actuator. All tests were conducted at 200 g and the over-consolidation ratio, OCR, for underlying clay was at least 1.5.

**Testing Procedure**

A total of 15 spudcan penetration tests were performed on medium loose sand overlying clay with sand thickness $H_s$ of 16, 25 and 30 mm. Five tests were conducted at each height, as detailed in Table 1. The ratio of $H_s/D$ was then between 0.16 and 1.0, which covers the range of practical interest as no
punch-through failures have been reported for $H/D > 1$. The first five tests were performed with a sand thickness of 30 mm. Following these tests the sand was further scraped back, to 25 mm and then to 16 mm (the bottom clay was re-consolidated under 200 g overnight after each scraping process), allowing tests to be performed at three sand thicknesses. At each stage the sand was removed over the entire drum channel, but the tests were conducted in different and untouched sites.

The relative density, $I_D$, of the sand layer was determined by extracting four samples from equidistant radial locations in the channel using 60 mm diameter sampling tubes after surcharging and before the tests (at 1 g). The samples were collected from the bed carefully ensuring minimal disturbance, and yielded an average relative density of 43%, with a standard deviation of 7%, indicating relatively uniform medium loose sand. The submerged unit weight of the sand, $\gamma_s$, was measured to be 10.0 kN/m$^3$. The submerged unit weight of the clay, $\gamma_c$, was measured directly on 20 mm diameter samples extracted by a tube sampler, which was 7.1 kN/m$^3$ on average.

The spudcans were loaded using displacement control at a constant penetration rate. The penetration rates were determined such that drained behavior in sand and undrained behavior in clay was attained. The following normalized penetration rate, $V$, was widely adopted to describe the drainage condition (Finnie and Randolph, 1994)

$$V = \frac{vD}{c_v}$$

(1)

where $v$ is the penetration velocity of foundation, $D$ is the foundation diameter and $c_v$ is the consolidation coefficient. For undrained conditions in clay there is a transition range of $30 < V < 300$ over which partial drainage are minimized (Finnie and Randolph, 1994). The dimensionless velocity $V$ was maintained as 120 in the clay ($c_v = 2$ m$^2$/year, Stewart (1992)) for all tests by varying the penetration velocity accordingly. Thus, the penetration velocities, $v$, for $D = 30$ mm and 100 mm were 0.254 mm/s and 0.076 mm/s respectively. The silica sand has been estimated to have a $c_v$ of at least 60,000 m$^2$/year (Lee, 2009) and therefore, $V$ was less than 0.01 in the sand layer for the penetration rates and spudcan sizes used. This ensured fully drained behaviour in the sand layer.
To obtain the undrained shear strength profile of clay layer, T-bar penetrometer tests were performed on the clay layer in isolation following careful removal of the upper sand layer after all of the spudcan penetration tests had been completed. This was intended to eliminate the influence of entrapped sand beneath the penetrometer and avoid potential damage to the penetrometer that may have occurred if it was penetrated through the sand layer. An intermediate roughness T-bar factor of 10.5 was assumed. Given that the OCR increased as the sand was scraped away at intervals during the test schedule to allow for thinner sand thickness, the shear strength profile of clay measured with the sand removed was calculated using the following relationship to account for the impact of changes in OCR to the shear strength (Koutsofias and Ladd, 1985)

$$\frac{s_u}{\sigma'_v} = aOCR^b$$  \hspace{1cm} (2)

where $s_u$ is the undrained shear strength, $\sigma'_v$ is the vertical effective stress, and $a$ and $b$ are fitting parameters. Two example T-bar tests from different locations within the drum channel are presented in Fig. 2 indicating excellent sample uniformity. The OCR profiles for each of the three layer heights were calculated using the measured effective unit weights of the sand and clay layers, prototype dimensions and the consolidation g-level. The best fit of Eq. 2 to the T-bar penetrometer profiles for all three sand layer heights tested was found with values for $a$ and $b$ of 0.16 and 0.74, respectively. Thus, the sand-clay interface shear strengths and shear strength gradients for the underlying clay layers tested were estimated using linear best fits to the non-linear profiles estimated using Eq. (2) and are summarized in Table 1. In the following, all experimental results are reported with prototype dimensions.

**Results and Discussion**

**Penetration Resistance Profiles**

The nominal penetration resistance, $q_{nom}$, profiles (penetration force normalized by the maximum bearing area of spudcan) for 15 medium loose sand overlying clay centrifuge tests are shown in Fig. 3.
They are grouped for different sand thickness. The displacement measurements are zeroed upon full embedment of the spigot (i.e. spudcan embedded until a depth measured from the tip of the spigot equal to \( t_1 + t_2 \) given in Table 1) as illustrated in Fig. 1. In general, both potential for punch-through and rapid leg run (see Fig. 3) are observed in these nominal penetration resistance profiles, indicating potential risk for spudcan installation on this type of soil stratigraphy. Punch-through and rapid leg run might occur when there is a rapid vertical spudcan displacement. For the case of ‘punch-through’ this is the result of an obvious reduction in the penetration resistance profile, while for rapid leg run the rapid displacement may stem from a period of nearly constant \( q_{\text{peak}} \) in the penetration resistance profile. Generally, punch-through is more likely to occur for larger \( H_s/D \) ratios and rapid leg run is prone for lower ratios of \( H_s/D \). Rapid leg run is potentially just as dangerous as punch-through since the uncontrolled displacements shown here are as large as 0.3\( D - 0.7D \). Fig. 4 presents selected typical nominal penetration resistance profiles for two pairs of spudcan penetration tests on dense and medium loose sand overlying clay (noting that the \( I_D = 92\% \) cases presented are the data of Lee (2009)). These profiles have been chosen since Fig. 4(a) and (c) and Fig. 4(b) and (d) exhibit identical \( D \), very similar \( H_s \), and consequently very close values of \( H_s/D \). Comparison of these penetration resistance profiles provides insight into the impact of various parameters on the peak penetration resistance and the potential of hazardous failure.

The comparisons of Fig. 4(a) and (b) and Fig. 4(c) and (d) demonstrate the impact of \( H_s/D \) on the nominal penetration resistance profiles. For both dense and loose sands \( q_{\text{peak}} \) reduces with \( H_s/D \). For dense sand with \( H_s/D = 0.78 \), the \( q_{\text{peak}} \) is 620 kPa, while it is 430 kPa for \( H_s/D = 0.44 \). The reduction of \( q_{\text{peak}} \) for medium loose sand is not so obvious, but still has a value of 15% for \( H_s/D = 0.43 \) compared with \( H_s/D = 0.75 \). This is because during the mobilization of \( q_{\text{peak}} \), for high \( H_s/D \), the influence zone is mainly confined to the sand layer, which would contribute to a large \( q_{\text{peak}} \). For the dense sand tests in Fig. 4(a) and (b), the reduction of \( H_s/D \) decreases the magnitude of the peak penetration resistance \( q_{\text{peak}} \) and also the potential length of the uncontrolled vertical displacement. For the medium loose sand tests in Fig. 4(c) and (d), the impact of reducing \( H_s/D \) is to change the
potential of failure from punch-through to rapid leg run. This is further confirmed by the other
medium loose sand tests presented in Fig. 3.

Comparison of Fig. 4(a) and (c) and Fig. 4(b) and (d) highlights the impact of \( I_D \) on the failure mode. For high \( H_s/D \), in Fig. 4(a) and (c), reducing the \( I_D \) changes the penetration resistance from a peaked and sudden failure, with significant rapid post-peak resistance reduction, to a more progressive failure with attenuated post-peak resistance reduction. For low \( H_s/D \), in Fig. 4(b) and (d), the same trend is evident except that the medium loose sand failure potential becomes a rapid leg run rather than punch-through.

This indicates that punch-through or rapid leg run failure is a potential problem for sand overlying clay stratigraphies involving sand from medium loose to dense states, since even in Fig. 4(d), which exhibits the smallest \( q_{peak} \), the potential for uncontrolled rapid leg run was observed. As a result, the failure stress dependent model proposed by Lee et al. (2009) for dense sand overlying clay is developed in this paper to accurately predict \( q_{peak} \) for problems involving sand from medium loose to dense states.

**Peak Penetration Resistance**

Fig. 5 presents the peak penetration resistance, \( q_{peak} \), versus the widest cross-sectional area for each of the spudcans tested. The data are grouped in accordance with the thickness and relative density of the sand layer. Fig. 5 illustrates that the general variations of the peak penetration resistances with the widest cross-sectional areas may be fitted with power law equations. Specific equations are not given for these fits since they are only intended to demonstrate trends in the results.

The bearing capacities of the spudcan for modern jack-ups are reported to be in the range of 200 to 600 kPa (Osborne et al. 2008). The experimentally measured peak penetration resistances shown in Fig. 5 are within this range, which suggests that the current centrifuge model tests were appropriately scaled to calibrate the proposed failure stress dependent model.

**Depth of Peak Penetration Resistance**
In addition to the peak penetration resistance \( q_{\text{peak}} \), the depth at which the peak penetration resistance occurs must be predicted, since both are necessary for providing a full penetration resistance profile for spudcan penetration on sand overlying clay. Based on centrifuge tests on dense sand overlying clay conducted at UWA and at the National University of Singapore (NUS), Teh et al. (2010) proposed that the effective sand thickness, \( H_{\text{eff}} \), at mobilisation of \( q_{\text{peak}} \) was equal to 0.88\( H_s \). The depth of penetration required to mobilise the peak penetration resistance, \( d_{\text{peak}} \) (\( d_{\text{peak}} = H_s - H_{\text{eff}} \)), is therefore 0.12\( H_s \). Fig. 6 is a summary of the correlation between \( H_{\text{eff}}/D \) and \( H_s/D \) for all the centrifuge tests listed in Table 1 and 2, except the beam centrifuge test of Lee (2009) of which the penetration resistance profiles were not available. The relationship proposed by Teh et al. (2010) is consistent for both UWA and NUS geometries of spudcan and the soil properties reported in Table 1 and 2. Thus the depth of peak penetration resistance relative to the lowest elevation of the spudcan widest cross-sectional area may be expressed with confidence as:

\[
d_{\text{peak}} = 0.12H_s
\]

**Failure Stress Dependent Prediction Model**

**Performance of Original Failure Stress Dependent Model**

As shown in Fig. 7, Lee et al. (2009) proposed an analytical model, which assumes that the peak penetration resistance occurs when a sand frustum with dispersion angle (the angle between assumed slip surface and vertical plane) equal to the angle of dilation, \( \psi \), is pushed into the underlying clay. Hence, \( q_{\text{peak}} \) is the sum of the frictional resistance in the sand, the bearing capacity of the underlying clay and the weight of the sand frustum. The operative friction and dilation angles are related to \( q_{\text{peak}} \) using a modified form of Bolton’s (1986) empirical relationships:

\[
I_R = I_D (Q - \ln(p')) - 1 \quad 0 < I_R < 4
\]

\[
\phi' - \phi_{cv} = mI_R
\]
where $I_R$ is a dilatancy indicator in degree, $Q$ is the natural logarithm of the grain crushing strength expressed in kPa, $p'$ is the mean effective stress, $\phi'$ is the operative friction angle, $\phi_{cv}$ is the critical state friction angle and $m$ is a constant. Lee (2009) used centrifuge model tests on dense sand overlying clay and accompanying small-strain finite element simulations to back-analyze a best fit value for $m$ of 2.65. The authors also performed similar simulations of the medium loose sand overlying clay tests presented in this paper with good comparability with the experimental measurements, providing confidence that a value for $m$ of 2.65 was appropriate irrespective of the relative density of the sand layer.

In Lee’s analytical model, a distribution factor, $D_F$, is defined to relate the local stress along the failure surface to the average vertical stress, or more specifically the ratio of the vertical effective stress at the slip surface to the mean vertical effective stress. The distribution factor depends on the ratio $H_s/D$ of flat or spudcan foundations and bilinear equations were proposed to depict the above relationship.

For current tests for medium loose sand layers, optimized $D_F$ values were derived by varying $D_F$ until the $q_{peak}$ predicted by the original model of Lee et al. (2009) was equal to the measured. The optimised $D_F$ values are plotted against $H_s/D$ in Fig. 8(a) alongside the calculated resistance divided by the experimental resistance ($q_{peak,\text{calculated}}/q_{peak,\text{measured}}$) in Fig. 8(b). The bilinear variations of $D_F$ with $H_s/D$ suggested by Lee et al. (2009) are plotted in Fig. 8 as well. Some skew of the regression line is evident in Fig. 8(b), particularly with smaller $H_s/D$, which means the original model underestimates the peak penetration resistance for smaller $H_s/D$. This is further verified by Fig. 8(a) as the bilinear $D_F$ equations do not capture the trend well, especially for cases when $H_s/D < 0.3$. This is not unexpected since the above failure mechanism and bilinear $D_F$ equations in its original state was calibrated solely using experimental data for spudcans in a single height ($H_s = 6.2$ m) of dense sand ($I_D = 92\%$) overlying clay. The original mechanism was validated, and not calibrated, using data from
only three tests performed on loose sand overlying clay reported in the literature. In addition, the embedment depth achieved during mobilization of \( q_{\text{peak}} \), is not accounted for.

**Modification of the Failure Stress Dependent Model**

To account for the embedment depth at failure the original mechanism was modified, as shown in Fig. 9. In this modified failure mechanism, the peak penetration resistance is derived following the same procedure as Lee (2009), but the embedment depth attained during mobilization of \( q_{\text{peak}} \) is taken into account. The \( D_f \) values are optimized and a new power relationship with \( H_s/D \) is proposed based on the modified failure mechanism. In brief, the problem is treated mathematically as a series of infinitesimally thin horizontal discs, which allows the following differential equation to be formulated

\[
\frac{\partial \bar{\sigma}_z'}{\partial z} + \frac{E \tan \psi}{(D/2 + z \tan \psi)} \sigma_z' - \gamma'_s = 0
\]  

(7)

where \( \sigma_z' \) is the average vertical stress in each horizontal disc at depth \( z \). The parameter \( E \) is adopted to simplify the algebra and taken as

\[
E = 2 \left[ 1 + D_f \left( \frac{\tan \phi^*}{\tan \psi} - 1 \right) \right]
\]

(8)

where \( \phi^* \) is a reduced friction angle caused by non-associated flow which can be expressed as

\[
\tan \phi^* = \frac{\sin \phi \cos \psi}{1 - \sin \phi \sin \psi}
\]

(9)

By assuming that \( D_f \) is constant with depth, Eq. (7) can be integrated to give

\[
\left( \frac{D}{2} + z \tan \psi \right)^E \cdot \frac{\gamma'_s \left( \frac{D}{2} + z \tan \psi \right)^{E+1}}{\tan \psi (E+1)} + C
\]

(10)
where $C$ is a constant which can be determined through the following critical condition. Referring to the conceptual model in Fig. 9, when the depth $z$ is equal to the effective sand thickness, $H_{eff}$, the mean vertical effective stress is equal to the bearing capacity of the underlying clay layer, thus $C$ can be expressed as

$$C = \left(\frac{D}{2} + H_{eff} \tan \psi\right) E \left(\frac{N_{c0} s_{u0} + q_0 + \gamma'_{s} H_{eff} + \gamma'_{s} d_{peak}}{E} - \frac{\gamma'_{s} \left(\frac{D}{2} + H_{eff} \tan \psi\right)}{E} \right)$$

(11)

where $N_{c0}$ is the bearing capacity factor of clay at foundation base, which is obtained using the relationship proposed by Houlsby and Martin (2003) for circular foundations with shear strength increasing linearly with depth; $s_{u0}$ is the undrained shear strength of the clay at the sand-clay interface and $q_0$ is the effective overburden pressure at the depth of the foundation.

By substituting Eq. (11) into Eq. (10), the mean vertical effective stress can be expressed as:

$$\bar{\sigma}'_v = \frac{\gamma'_{s} \left(\frac{D}{2} + z \tan \psi\right)}{\tan \psi (E + 1)} + \left(\frac{D}{2} + H_{eff} \tan \psi\right) E \left(\frac{N_{c0} s_{u0} + q_0 + \gamma'_{s} H_{eff} + \gamma'_{s} d_{peak}}{E} - \frac{\gamma'_{s} \left(\frac{D}{2} + H_{eff} \tan \psi\right)}{E} \right)$$

(12)

According to Fig. 9, the spudcan penetration depth $z$ is measured from the depth where the peak penetration resistance occurs and the peak penetration resistance can be obtained by setting $z$ equal to zero. As discussed above, $H_{eff} = 0.88 H_s$ for both tests involving dense and loose sand layers, by substituting $\bar{\sigma}'_v$ with $q_{peak}$ and input the values for $d_{peak}$ and $H_{eff}$ in Eq. (12), the peak penetration resistance is thus expressed in terms of $H_s$: 

$$\bar{\sigma}'_v = q_{peak}$$
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\[ q_{\text{peak}} = (N_{\text{c0}} s_{\text{u0}} + q_0 + 0.12 \gamma'_{\text{s}} H_s) \left(1 + \frac{1.76 H_s}{D} \tan \psi \right)^E \]

\[ + \frac{\gamma'_{\text{s}} D}{2 \tan \psi (E+1)} \left[1 - \left(1 - \frac{1.76 H_s}{D} E \tan \psi \right) \left(1 + \frac{1.76 H_s}{D} \tan \psi \right)^E \right] \]

for cases where \( \phi' > \phi_{cv} \). Similarly, for cases where \( \phi' = \phi_{cv} \), the peak penetration resistance can be calculated as:

\[ q_{\text{peak}} = (N_{\text{c0}} s_{\text{u0}} + q_0 + 0.12 \gamma'_{\text{s}} H_s) e^{E_0} + 0.88 \gamma'_{\text{s}} H_s \left[e^{E_0} \left(1 - \frac{1}{E_0} \right) + \frac{1}{E_0} \right] \]

where \( E_0 \) is equal to

\[ E_0 = 3.52 D_f \sin \phi_{cv} \frac{H_s}{D} \]

In Eq. (4), the mean effective stress \( p' \) is substituted with \( q_{\text{peak}} \) in Eq. (13) and through an iterative procedure using Eqs. (4) to (6) and (13) in a spreadsheet analysis (for example in MS Excel), this approach allows the operative friction angle and dilatancy (and thus dispersion angle of the sand frustum) to be related to the stress level at failure rather than the initial state. This method is advantageous as it avoids the use of design charts and sensitivity analysis can be conducted with ease.

Based on the modified failure stress dependent model and with the benefit of the additional experimental data presented, the distribution factor was recalibrated and optimized in terms of a wide range of spudcan geometries and of soil conditions incorporating both loose and dense sand overlying clay. The optimised \( D_f \) for the additional fifteen centrifuge tests for medium loose sand and tests for the dense sand by Lee (2009) are presented in Fig. 10(a). It is observed that the relationship between \( D_f \) and \( H_s/D \) is non-linear and better fitted with the power law.

\[ D_f = 0.642 \left(\frac{H_s}{D}\right)^{-0.576} \text{ as } 0.16 \leq \frac{H_s}{D} \leq 1.0 \]
Using the original model and linear relationships proposed by Lee et al. (2009) the coefficient of determination, $R^2$, is 0.77 for experimental data in Fig. 10, whilst $R^2 = 0.94$ using the modified model and the power relationship in Eq. (16). For low $H/D$, the embedded volume of the spudcan during mobilisation of $q_{peak}$ is a far larger proportion of the volume of the inverted truncated cone in the modified failure mechanism than that for high $H/D$. This embedded volume causes increasing lateral stress, and then the larger values of $D_F$. The embedded volume of the spudcan can also be expressed in terms of $H/D$ using a similar power relationship. Although it is not possible to link $D_F$ directly to the embedded volume of the spudcan at $q_{peak}$, (given that the increase in mean stress at the failure surface of the proposed failure mechanism is highly unlikely to be directly proportional to the volume of sand displaced during spudcan embedment) the similar power relationship would suggest that the non-linear relationship proposed in Eq. (16) to describe $D_F$ for spudcans is logical.

Similar to Fig. 8(b), the scattered markers in Fig. 10(b) shows the predictions for both loose and dense sand tests based on the modified mechanism and power relationship of $D_F$. There is reduced skew for the whole range of $H/D$ of practical interest. This is because the embedment depth during the mobilization of peak penetration resistance is accounted for in the modified failure mechanism and the new $D_F$ relationship is calibrated for a larger range of spudcan diameters and soil properties. More tests are needed to investigate the suitability of the $D_F$ relationship for different spudcan shapes (conical angles).

**Performance of the Modified Model in Predicting $q_{peak}$**

To further validate the performance of the modified and recalibrated model, three series of additional centrifuge test data for the penetration of spudcans into sand overlying normally or lightly over-consolidated clay have been compared. These additional tests comprise of seven tests by Teh (2007) in the NUS centrifuge, three tests by Teh (2007) in the UWA beam centrifuge and five tests by Lee (2009) in the UWA beam centrifuge. Table 1 and 2 contain a summary of the relevant geometric and material parameters of these tests, as well as the experimental results. All the data used in this validation were derived from tests with siliceous sand; consequently $Q$ in Eq. (4) was assumed as 10
The performance of the modified model is compared to the primary (based on the load spread method) and alternative (based upon the punching shear method) recommendations of ISO (2012). For each method, the measured and calculated peak penetration resistance predictions are presented with $q_{\text{peak, calculated}}$ against $q_{\text{peak, measured}}$ and $q_{\text{peak, calculated}}/q_{\text{peak, measured}}$ against $H_s/D$, as shown in Fig. 11. A linear regression line is used in the $q_{\text{peak, calculated}}/q_{\text{peak, measured}}$ figure to identify any apparent trend in performance of the calculation with respect to $H_s/D$. Table 3 provides a summary of key performance indicators such as mean, maximum, minimum, standard deviation and skew, where $\theta = \arctan(s)$ and $s$ is the slope of the regression line.

For both the ISO (2012) primary and alternative recommendations conservative predictions of $q_{\text{peak}}$ are obtained, with the majority of the predicted peak penetration resistances less than 60% of the measured peak penetration resistances. The reason is that both methods ignore the properties of the sand: the load spread factor is not related to the sand properties in the primary recommendation, and the frictional resistance through the sand is expressed in terms of the normalized shear strength of the underlying clay layer in the alternative recommendation. The alternative recommendation made by ISO (2012) based on the punching shear mechanism actually performs better than the primary recommendation based on the load-spread method. Referring back to Fig. 4 demonstrates the implication of this conservative prediction of $q_{\text{peak}}$. For both medium loose and dense sands, such conservatism would lead to gross under-estimation of the potential impact of both punch-through and rapid leg run as the depth over which the event may occur would also be underestimated. The skew angles presented in Fig. 11 and Table 3 demonstrate that the methods from ISO (2012) recommendations exhibit significant bias in performance, with worsening predictions for larger $H_s/D$ for the load spread method. This is because at higher $H_s/D$ ratios the thicker sand thickness leads to the capacity of resistance generated by the sand being a larger proportion of $q_{\text{peak}}$. Hence, by ignoring
the contribution of the sand layer in the load spread method the predictions worsen with increasing $H_s/D$.

In contrast to the ISO (2012) recommendations, the modified failure stress dependent model with the recalibrated $D_F$ provides an average of all the predictions of $q_{\text{peak, calculated}}/q_{\text{peak, measured}}$ of 1.01 and a standard deviation of 0.11. All predictions, apart from test NUS_F5 from Teh (2007), are within ±20% of the measured values. The significantly less skew with respect to $H_s/D$ for the predictions indicates that the modified failure stress dependent model is capable of accounting for changes in stratigraphy far more effectively than the ISO methods. This is because the failure stress is highly dependent upon sand thickness and foundation size as demonstrated in Fig. 5, and the operative friction angle and angle of inclination of the inverted truncated cone mechanism is related to the failure stress in the modified failure stress dependent model. By adopting the modified failure stress dependent model to improve the accuracy of the estimation of $q_{\text{peak}}$, the uncertainty and risk associated with spudcan installation in sand overlying clay stratigraphies may be reduced.

**Conclusions**

Fifteen centrifuge tests have been conducted within a drum centrifuge to investigate spudcan foundation behavior on medium loose sand overlying clay, representing the first comprehensive investigation of punch-through or rapid leg-run potential for medium loose sand overlying clay. The tests covered different prototype sand thicknesses in the range of 3.2 to 6 m and spudcan diameters in the range of 6 to 20 m, corresponding to $H_s/D$ ratios of 0.16 to 1. This covers the range of practical interest for punch-through failure of jack-up platforms. This new data was combined with the data for spudcan penetrating dense sand overlying clay from Lee (2009) to allow recalibration of the modified failure stress dependent model. Interpretation of this data has led to the following conclusions:

1. The potential for catastrophic punch-through and rapid leg run of spudcans, already demonstrated for dense sand overlying clay, is also a potential problem for medium loose sand overlying clay sites.
2. The depth of occurrence of $q_{\text{peak}}$ has been further confirmed experimentally to be a function of $H_s$ for the range of $H_s/D$ of practical interest. Coupling the depth of occurrence with accurate prediction of $q_{\text{peak}}$ provides the first step in predicting the risk of punch-through failure for sand overlying clay sites.

3. The failure stress dependent model of Lee et al. (2009) for predicting $q_{\text{peak}}$ on sand overlying clay has been modified to account for mobilization induced embedment. This modified mechanism has been used to derive an equation to describe $q_{\text{peak}}$ in terms of the undisturbed sand thickness.

4. A new relationship has been proposed for $D_F$, which is used to relate the stress at the failure surface to the average vertical stress in the modified failure stress dependent model. This provides improved prediction of $q_{\text{peak}}$ over a larger range of sand thickness to spudcan diameter ratios $H_s/D$ as well as sand relative densities. At this juncture the new relationship has been calibrated and validated only for spudcan shapes similar to that tested here.

5. The modified failure stress dependent model, which is based on a kinematically admissible failure mechanism and accounts for the embedment depth caused by mobilization of $q_{\text{peak}}$, was shown to be capable of accurately predicting the peak penetration resistance $q_{\text{peak}}$ for both loose and dense sand overlying clay.

6. The performance of the modified failure stress dependent model has been compared with the current recommended practice of the ISO (2012) primary and alternative recommendations, and it was demonstrated that the modified model provides more accurate prediction of $q_{\text{peak}}$ with less bias with relation to $H_s/D$ for a wide range of dense and loose sand over clay sites.

In summary, when used to back-calculate centrifuge data, the use of the ISO (2012) $q_{\text{peak}}$ prediction methods significantly underestimates the potential for punch-through during spudcan penetration on sand overlying clay. The modified failure stress dependent model improves the $q_{\text{peak}}$ predictions and its adoption for field conditions offshore has the potential to better predict the potential for punch-
through or rapid leg run events during spudcan installation on sand overlying clay. This would significantly reduce the risk associated with operating jack-up platforms in offshore locations with sand overlying clay soil stratigraphy.

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